## DRAFT

# Geometry EOC Item Specifications 

The draft Florida Standards Assessments (FSA) Test Item Specifications (Specifications) are based upon the Florida Standards and the Florida Course Descriptions as provided in CPALMs. The Specifications are a resource that defines the content and format of the test and test items for item writers and reviewers. Each grade-level and course Specifications document indicates the alignment of items with the Florida Standards. It also serves to provide all stakeholders with information about the scope and function of the FSA.

## Item Specifications Definitions

Also assesses refers to standard(s) closely related to the primary standard statement.

Clarification statements explain what students are expected to do when responding to the question.

Assessment limits define the range of content knowledge and degree of difficulty that should be assessed in the assessment items for the standard.

Item types describe the characteristics of the question.
Context defines types of stimulus materials that can be used in the assessment items.

## Florida Standards Assessments

## Modeling Cycle

The basic modeling cycle involves (1) identifying variables in the situation and selecting those that represent essential features, (2) formulating a model by creating and selecting geometric, graphical, tabular, algebraic, or statistical representations that describe relationships between the variables, (3) analyzing and performing operations on these relationships to draw conclusions, (4) interpreting the results of the mathematics in terms of the original situation, (5) validating the conclusions by comparing them with the situation, and then either improving the model or, if it is acceptable, (6) reporting on the conclusions and the reasoning behind them. Choices, assumptions, and approximations are present throughout this cycle.
http://www.cpalms.org/Standards/mafs modeling standards.aspx

## Mathematical Practices:

The Mathematical Practices are a part of each course description for Grades 3-8, Algebra 1, and Geometry. These practices are an important part of the curriculum. The Mathematical Practices will be assessed throughout.
\(\left.$$
\begin{array}{|l}\begin{array}{l}\text { Make sense of problems and persevere in solving them. } \\
\\
\text { Mathematically proficient students start by explaining to themselves the } \\
\text { meaning of a problem and looking for entry points to its solution. They } \\
\text { analyze givens, constraints, relationships, and goals. They make } \\
\text { conjectures about the form and meaning of the solution and plan a } \\
\text { solution pathway rather than simply jumping into a solution attempt. } \\
\text { They consider analogous problems, and try special cases and simpler } \\
\text { forms of the original problem in order to gain insight into its solution. } \\
\text { They monitor and evaluate their progress and change course if necessary. } \\
\text { Older students might, depending on the context of the problem, } \\
\text { transform algebraic expressions or change the viewing window on their } \\
\text { graphing calculator to get the information they need. Mathematically } \\
\text { proficient students can explain correspondences between equations, } \\
\text { verbal descriptions, tables, and graphs or draw diagrams of important } \\
\text { features and relationships, graph data, and search for regularity or trends. } \\
\text { Younger students might rely on using concrete objects or pictures to help } \\
\text { conceptualize and solve a problem. Mathematically proficient students } \\
\text { check their answers to problems using a different method, and they } \\
\text { continually ask themselves, "Does this make sense?" They can understand } \\
\text { the approaches of others to solving complex problems and identify } \\
\text { correspondences between different approaches. }\end{array} \\
\begin{array}{ll}\text { Reason abstractly and quantitatively. }\end{array} \\
\begin{array}{ll}\text { Mathematically proficient students make sense of quantities and their } \\
\text { relationships in problem situations. They bring two complementary }\end{array}
$$ <br>
abilities to bear on problems involving quantitative relationships: the <br>
ability to decontextualize-to abstract a given situation and represent it <br>

symbolically and manipulate the representing symbols as if they have a\end{array}\right\}\)| life of their own, without necessarily attending to their referents-and |
| :--- |
| the ability to contextualize, to pause as needed during the manipulation |
| process in order to probe into the referents for the symbols involved. |
| Quantitative reasoning entails habits of creating a coherent |
| representation of the problem at hand; considering the units involved; |
| attending to the meaning of quantities, not just how to compute them; |
| and knowing and flexibly using different properties of operations and |
| objects. |


| MAFS.K12.MP.3.1: | Construct viable arguments and critique the reasoning of others. <br> Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and-if there is a flaw in an argument-explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments. |
| :---: | :---: |
| MAFS.K12.MP.4.1: | Model with mathematics. <br> Mathematically proficient students can apply the mathematics they know to solve problems arising in everyday life, society, and the workplace. In early grades, this might be as simple as writing an addition equation to describe a situation. In middle grades, a student might apply proportional reasoning to plan a school event or analyze a problem in the community. By high school, a student might use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another. Mathematically proficient students who can apply what they know are comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later. They are able to identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas. They can analyze those relationships mathematically to draw conclusions. They routinely interpret their mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose. |

## Use appropriate tools strategically.

Mathematically proficient students consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software. Proficient students are sufficiently familiar with tools appropriate for their grade or course to make sound decisions about when each of these tools might be helpful, recognizing both the insight to be gained and their limitations. For example, mathematically proficient high school students analyze graphs of functions and solutions generated using a graphing calculator. They detect possible errors by strategically using estimation and other mathematical knowledge. When making mathematical models, they know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data. Mathematically proficient students at various grade levels are able to identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems. They are able to use technological tools to explore and deepen their understanding of concepts.

## Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

## Look for and make use of structure.

Mathematically proficient students look closely to discern a pattern or structure. Young students, for example, might notice that three and seven more is the same amount as seven and three more, or they may sort a collection of shapes according to how many sides the shapes have. Later, students will see $7 \times 8$ equals the well remembered $7 \times 5+7 \times 3$, in preparation for learning about the distributive property. In the expression $x^{2}+9 x+14$, older students can see the 14 as $2 \times 7$ and the 9 as $2+7$. They recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. They also can step back for an overview and shift perspective. They can see complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. For example, they can see 5 -$3(x-y)^{2}$ as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers $x$ and $y$.
Look for and express regularity in repeated reasoning.
Mathematically proficient students notice if calculations are repeated, and look both for general methods and for shortcuts. Upper elementary students might notice when dividing 25 by 11 that they are repeating the same calculations over and over again, and conclude they have a repeating decimal. By paying attention to the calculation of slope as they
MAFS.K12.MP.8.1: repeatedly check whether points are on the line through $(1,2)$ with slope 3 , middle school students might abstract the equation $(y-2) /(x-1)=3$. Noticing the regularity in the way terms cancel when expanding $(x-1)(x+$ 1), $(x-1)\left(x^{2}+x+1\right)$, and $(x-1)\left(x^{3}+x^{2}+x+1\right)$ might lead them to the general formula for the sum of a geometric series. As they work to solve a problem, mathematically proficient students maintain oversight of the process, while attending to the details. They continually evaluate the reasonableness of their intermediate results.

## Technology-Enhanced Item Descriptions:

The Florida Standards Assessments (FSA) are composed of test items that include traditional multiple-choice items, items that require the student to type or write a response, and technology-enhanced items (TEI). Technology-enhanced items are computer-delivered items that require the student to interact with test content to select, construct, and/or support their answers.

Currently, there are nine types of TEls that may appear on computer-based assessments for FSA Mathematics. For students with an IEP or 504 plan that specifies a paper-based accommodation, TEls will be modified or replaced with test items that can be scanned and scored electronically.

Any of the item types may be combined into a single item with multiple parts called a multiinteraction item. The student will interact with different item types within a single item. Each part could be a different item type. For paper-based assessments, this item type may be replaced with a modified version of the item that can be scanned and scored electronically, or replaced with another item type that assesses the same standard and can be scanned and scored electronically.

For samples of each of the item types described below, see the FSA Practice Tests.

## Technology-Enhanced Item Types - Mathematics

1. Editing Task Choice - The student clicks a highlighted word, phrase, or blank, which reveals a drop-down menu containing options for correcting an error as well as the highlighted word or phrase as it is shown in the sentence to indicate that no correction is needed. The student then selects the correct word or phrase from the drop-down menu. For paperbased assessments, the item is modified so that it can be scanned and scored electronically. The student fills in a bubble to indicate the correct word or phrase.
2. Editing Task - The student clicks on a highlighted word or phrase that may be incorrect, which reveals a text box. The directions in the text box direct the student to replace the highlighted word or phrase with the correct word or phrase. For paper-based assessments, this item type may be replaced with another item type that assesses the same standard and can be scanned and scored electronically.
3. Hot Text -
a. Selectable Hot Text - Excerpted sentences from the text are presented in this item type. When the student hovers over certain words, phrases, or sentences, the options highlight. This indicates that the text is selectable ("hot"). The student can then click
on an option to select it. For paper-based assessments, a "selectable" hot text item is modified so that it can be scanned and scored electronically. In this version, the student fills in a bubble to indicate a selection.
b. Drag-and-Drop Hot Text - Certain numbers, words, phrases, or sentences may be designated "draggable" in this item type. When the student hovers over these areas, the text highlights. The student can then click on the option, hold down the mouse button, and drag it to a graphic or other format. For paper-based assessments, drag-and-drop hot text items will be replaced with another item type that assesses the same standard and can be scanned and scored electronically.
4. Open Response - The student uses the keyboard to enter a response into a text field. These items can usually be answered in a sentence or two. For paper-based assessments, this item type may be replaced with another item type that assesses the same standard and can be scanned and scored electronically.
5. Multiselect - The student is directed to select all of the correct answers from among a number of options. These items are different from Multiple Choice items, which allow the student to select only one correct answer. These items appear in the online and paperbased assessments.
6. Graphic Response Item Display (GRID) - The student selects numbers, words, phrases, or images and uses the drag-and-drop feature to place them into a graphic. This item type may also require the student to use the point, line, or arrow tools to create a response on a graph. For paper-based assessments, this item type may be replaced with another item type that assesses the same standard and can be scanned and scored electronically.
7. Equation Editor - The student is presented with a toolbar that includes a variety of mathematical symbols that can be used to create a response. Responses may be in the form of a number, variable, expression, or equation, as appropriate to the test item. For paperbased assessments, this item type may be replaced with a modified version of the item that can be scanned and scored electronically or replaced with another item type that assesses the same standard and can be scanned and scored electronically.
8. Matching Item - The student checks a box to indicate if information from a column header matches information from a row. For paper-based assessments, this item type may be replaced with another item type that assesses the same standard and can be scanned and scored electronically.
9. Table Item - The student types numeric values into a given table. The student may complete the entire table or portions of the table depending on what is being asked. For paper-based assessments, this item type may be replaced with another item type that assesses the same standard and can be scanned and scored electronically.

## Reference Sheets:

- Reference sheets will be available as online references (in a pop-up window). A paper version will be available for paper-based tests.
- Reference sheets with conversions will be provided for FSA Mathematics assessments in Grades 4-8 and EOC Mathematics assessments.
- There is no reference sheet for Grade 3.
- For Grades 4, 6, 7, and Geometry, some formulas will be provided on the reference sheet.
- For Grade 5 and Algebra 1, some formulas may be included with the test item if needed to meet the intent of the standard being assessed.
- For Grade 8, no formulas will be provided; however, conversions will be available on a reference sheet.

| Grade | Conversions | Some Formulas |
| :---: | :---: | :---: |
| 3 | No | No |
| 4 | On Reference Sheet | On Reference Sheet |
| 5 | On Reference Sheet | With Item |
| 6 | On Reference Sheet | On Reference Sheet |
| 7 | On Reference Sheet | On Reference Sheet |
| 8 | On Reference Sheet | No |
| Algebra 1 | On Reference Sheet | With Item |
| Geometry | On Reference Sheet | On Reference Sheet |


| MAFS.912.G-C.1.1 | Prove that all circles are similar. |
| :---: | :---: |
| Clarifications | Students will use a sequence of transformations to prove that circles are similar. <br> Students will use the measures of different parts of a circle to determine similarity. |
| Assessment Limits | Items should not require the student to use the distance or midpoint formula. <br> Items should not require the student to write an equation of a circle. <br> Items may require the student to be familiar with using the algebraic description $(x, y) \rightarrow(x+a, y+b)$ for a translation, and $(x, y) \rightarrow(k x, k y)$ for a dilation when given the center of dilation. Items may require the student to be familiar with the algebraic description for a 90-degree rotation about the origin, $(x, y) \rightarrow(-y, x)$, for a 180-degree rotation about the origin, $(x, y) \rightarrow(-x,-y)$, and for a 270-degree rotation about the origin, $(x, y) \rightarrow(y,-x)$. Items that use more than one transformation may ask the student to write a series of algebraic descriptions. <br> Items should not use matrices to describe transformations. |
| Stimulus Attributes | Circles should not be given in equation form. <br> Items may be set in a real-world or mathematical context. |
| Response Attribute | Items may require the student to use or choose the correct unit of measure. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-C.1.2 | Identify and describe relationships among inscribed angles, radii, and <br> chords. Include the relationship between central, inscribed, and <br> circumscribed angles; inscribed angles on a diameter are right angles; <br> the radius of a circle is perpendicular to the tangent where the radius <br> intersects the circle. |
| :--- | :--- |
| Clarification | Students will solve problems related to circles using the properties of <br> central angles, inscribed angles, circumscribed angles, diameters, <br> radii, chords, and tangents. |
| Assessment Limit | Items may include finding or describing the length of arcs when given <br> information. |
| Stimulus Attribute | Items may be set in a real-world or mathematical context. |
| Response Attribute | Items may require the student to use or choose the correct unit of <br> measure. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-C.1.3 | Construct the inscribed and circumscribed circles of a triangle, and <br> prove properties of angles for a quadrilateral inscribed in a circle. |
| :--- | :--- |
| Clarifications | Students will construct a circle inscribed inside a triangle. |
| Students will construct a circle circumscribed about a triangle. |  |
| Students will solve problems using the properties of inscribed and |  |
| circumscribed circles of a triangle. |  |
| Students will use or justify properties of angles of a quadrilateral that |  |
| is inscribed in a circle. |  |

\(\left.$$
\begin{array}{|l|l|}\hline \text { MAFS.912.G-C.2.5 } & \begin{array}{l}\text { Derive using similarity the fact that the length of the arc intercepted } \\
\text { by an angle is proportional to the radius, and define the radian } \\
\text { measure of the angle as the constant of proportionality; derive the } \\
\text { formula for the area of a sector. }\end{array} \\
\hline \text { Clarifications } & \begin{array}{l}\text { Students will use similarity to derive the fact that the length of the arc } \\
\text { intercepted by an angle is proportional to the radius, and define the } \\
\text { radian measure as the constant of proportionality. }\end{array}
$$ <br>
Students will apply similarity to solve problems that involve the <br>

length of the arc intercepted by an angle and the radius of a circle.\end{array}\right\}\) Students will derive the formula for the area of a sector.,$~$| Students will use the formula for the area of a sector to solve |
| :--- | :--- |
| problems. |


| MAFS.912.G-CO.1.1 | Know precise definitions of angle, circle, perpendicular line, parallel <br> line, and line segment, based on the undefined notions of point, line, <br> distance along a line, and distance around a circular arc. |
| :--- | :--- |
| Clarification | Students will use the precise definitions of angles, circles, <br> perpendicular lines, parallel lines, and line segments, basing the <br> definitions on the undefined notions of point, line, distance along a <br> line, and distance around a circular arc. |
| Assessment Limit | Items may be set in a real-world or mathematical context <br> Items may require the student to analyze possible definitions to <br> determine mathematical accuracy. |
| Stimulus Attributes | Items may require the student to use definitions for justifications <br> when choosing examples or nonexamples. |
| Response Attribute | Items may require the student to use properties of rotations, <br> reflections, and translations as steps to a formal definition. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |

Geometry EOC Item Specifications
Florida Standards Assessments

| MAFS.912.G-CO.1.2 <br> Also assesses MAFS.912.G-CO.1.4 | Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch). <br> Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. |
| :---: | :---: |
| Clarifications | Students will represent transformations in the plane. <br> Students will describe transformations as functions that take points in the plane as inputs and give other points as outputs. <br> Students will compare transformations that preserve distance and angle to those that do not. <br> Students will use definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments. |
| Assessment Limits | Items may require the student to be familiar with using the algebraic description $(x, y) \rightarrow(x+a, y+b)$ for a translation, and $(x, y) \rightarrow(k x, k y)$ for a dilation when given the center of dilation. Items may require the student to be familiar with the algebraic description for a 90-degree rotation about the origin, $(x, y) \rightarrow(-y, x)$, for a 180-degree rotation about the origin, $(x, y) \rightarrow(-x,-y)$, and for a 270-degree rotation about the origin, $(x, y) \rightarrow(y,-x)$. Items that use more than one transformation may ask the student to write a series of algebraic descriptions. <br> Items must not use matrices to describe transformations. <br> Items must not require the student to use the distance formula. <br> Items may require the student to find the distance between two points or the slope of a line. <br> In items that require the student to represent transformations, at least two transformations should be applied. |
| Stimulus Attributes | Items may be set in real-world or mathematical context. <br> Items may ask the student to determine if a transformation is rigid. <br> Items may ask the student to determine if steps that are given can be used to develop a definition of an angle, a circle, perpendicular lines, parallel lines, or line segments by using rotations, reflections, and translations. |


| Response Attributes | Items may require the student to give a coordinate of a transformed <br> figure. <br> Items may require the student to use a function, e.g., <br> $y=k(f(x+a))+b$, to describe a transformation. |
| :--- | :--- |
|  | Items may require the student to determine if a verbal description of <br> a definition is valid. <br> Items may require the student to determine any flaws in a verbal <br> description of a definition. |
| Items may require the student to be familiar with slope-intercept |  |
| form of a line, standard form of a line, and point-slope form of a line. |  |
| Items may require the student to give a line of reflection and/or a |  |
| degree of rotation that carries a figure onto itself. |  |
| Items may require the student to draw a figure using a description of |  |
| a translation. |  |

Geometry EOC Item Specifications
Florida Standards Assessments

| MAFS.912.G-CO.1.5 <br> Also assesses MAFS.912.G-CO.1.3 | Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another. <br> Given a rectangle, parallelogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself. |
| :---: | :---: |
| Clarifications | Students will apply two or more transformations to a given figure to draw a transformed figure. <br> Students will specify a sequence of transformations that will carry a figure onto another. <br> Students will describe rotations and reflections that carry a geometric figure onto itself. |
| Assessment Limits | Items should not require the student to find the distance between points. <br> Items may require the student to be familiar with using the algebraic description $(x, y) \rightarrow(x+a, y+b)$ for a translation, and $(x, y) \rightarrow(k x, k y)$ for a dilation when given the center of dilation. Items may require the student to be familiar with the algebraic description for a 90-degree rotation about the origin, $(x, y) \rightarrow(-y, x)$, for a 180-degree rotation about the origin, $(x, y) \rightarrow(-x,-y)$, and for a 270-degree rotation about the origin, $(x, y) \rightarrow(y,-x)$. Items that use more than one transformation may ask the student to write a series of algebraic descriptions. <br> Items must not use matrices to describe transformations. <br> In items in which the line of reflection is given, it must be in slopeintercept form. <br> In items in which the line of reflection is given, any form of a line may be used. If the line is not a vertical line or a horizontal line, then the line of reflection must be graphed as a dotted line. |
| Stimulus Attributes | Items may be set in a real-world or mathematical context. <br> Items may require the student to provide a sequence of transformations. <br> Items may require the student to determine if an attribute of a figure is the same after a sequence of transformations has been applied. |


| Response Attributes | Items may require the student to use a function, e.g., <br> $y=k(f(x+a))+b$, to describe a transformation. |
| :--- | :--- |
|  | Items may require the student to give a line of reflection and/or a <br> degree of rotation that carries a figure onto itself. <br> Items may require the student to draw a figure using a description of <br> a transformation. |
| Items may require the student to graph a figure using a description of |  |
| a rotation and/or reflection. |  |
| In items in which the student has to write the line of reflection, any |  |
| line may be used. |  |
| Items may require the student to be familiar with slope-intercept |  |
| form of a line, standard form of a line, and point-slope form of a line. |  |
| Items may require the student to write a line of reflection that will |  |
| carry a figure onto itself. |  |
| Items may require the student to give a degree of rotation that will |  |
| carry a figure onto itself. |  |



| Stimulus Attributes | Items may be set in a real-world or mathematcal context. <br> Items may require the student to determine the rigid motions that <br> show that two triangles are congruent. |
| :--- | :--- |
| Response Attributes | Items may ask the student to name corresponding angles and/or <br> sides. <br> Items may require the student to use a function, e.g., <br> $y=k(f(x+a))+b$, to describe a transformation. |
|  | In items in which the student must write the line of reflection, any <br> line may be used. <br> Items may require the student to be familiar with slope-intercept <br> form of a line, standard form of a line, and point-slope form of a line. |
| Items may require the student to name corresponding angles or |  |
| sides. |  |
| Items may require the student to determine the transformations |  |
| required to show a given congruence. |  |
| Calculator |  |
| Sample Item |  |
| Items may require the student to list sufficient conditions to prove |  |
| triangles are congruent. |  |
| Items may require the student to determine if given information is |  |
| sufficient for congruence. |  |
| Items may require the student to give statements to complete formal |  |
| and informal proofs. |  |
| Neutral |  |
| See Appendix A for the Practice Test items aligned to a standard in |  |
| this group. |  |


| MAFS.912.G-CO.3.9 | Prove theorems about lines and angles; use theorems about lines and angles to solve problems. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent; points on a perpendicular bisector of a line segment are exactly those equidistant from the segment's endpoints. |
| :---: | :---: |
| Clarifications | Students will prove theorems about lines. <br> Students will prove theorems about angles. <br> Students will use theorems about lines to solve problems. <br> Students will use theorems about angles to solve problems. |
| Assessment Limits | Items may assess relationships between vertical angles, special angles formed by parallel lines and transversals, angle bisectors, congruent supplements, congruent complements, and a perpendicular bisector of a line segment. <br> Items may have multiple sets of lines and angles. <br> Items may include narrative proofs, flow-chart proofs, two-column proofs, or informal proofs. <br> In items that require the student to justify, the student should not be required to recall from memory the formal name of a theorem. |
| Stimulus Attribute | Items may be set in a real-world or mathematical context. |
| Response Attributes | Items may require the student to give statements and/or justifications to complete formal and informal proofs. <br> Items may require the student to justify a conclusion from a construction. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test items aligned to this standard. |


| MAFS.912.G-CO.3.10 | Prove theorems about triangles; use theorems about triangles to <br> solve problems. Theorems include: measures of interior angles of a <br> triangle sum to $180^{\circ}$; base angles of isosceles triangles are congruent; <br> the segment joining midpoints of two sides of a triangle is parallel to <br> the third side and half the length; the medians of a triangle meet at a <br> point. |
| :--- | :--- |
| Clarifications | Students will prove theorems about triangles. <br> Students will use theorems about triangles to solve problems. |
| Assessment Limits | Items may assess theorems and their converses for interior triangle <br> sum, base angles of isosceles triangles, mid-segment of a triangle, <br> concurrency of medians, concurrency of angle bisectors, concurrency <br> of perpendicular bisectors, triangle inequality, and the Hinge <br> Theorem. <br> Items may include narrative proofs, flow-chart proofs, two-column <br> proofs, or informal proofs. |
| Stimulus Attribute | In items that require the student to justify, the student should not be <br> required to recall from memory the formal name of a theorem. |
| Response Attributes | Items may be set in a real-world or mathematical context. |
| Salculator | Items may require the student to give statements and/or <br> justifications to complete formal and informal proofs. |
| Items may require the student to justify a conclusion from a |  |
| construction. |  |

\(\left.$$
\begin{array}{|l|l|}\hline \text { MAFS.912.G-CO.3.11 } & \begin{array}{l}\text { Prove theorems about parallelograms; use theorems about } \\
\text { parallelograms to solve problems. Theorems include: opposite sides } \\
\text { are congruent, opposite angles are congruent, the diagonals of a } \\
\text { parallelogram bisect each other, and conversely, rectangles are } \\
\text { parallelograms with congruent diagonals. }\end{array} \\
\hline \text { Clarifications } & \begin{array}{l}\text { Students will prove theorems about parallelograms. } \\
\text { Students will use properties of parallelograms to solve problems. }\end{array} \\
\hline \text { Assessment Limits } & \begin{array}{l}\text { Items may require the student to be familiar with similarities and } \\
\text { differences between types of parallelograms (eg., squares and } \\
\text { rectangles). }\end{array} \\
& \begin{array}{l}\text { Items may require the student to identify a specific parallelogram. }\end{array}
$$ <br>
Items may assess theorems and their converses for opposite sides of <br>
a parallelogram, opposite angles of a parallelogram, diagonals of a <br>

parallelogram, and consecutive angles of a parallelogram.\end{array}\right\}\)| Items may assess theorems and their converses for rectangles and |
| :--- |
| rhombuses. |
| Calculator |
| Sample Item |
| Response Attributes may include narrative proofs, flow-chart proofs, two-column |
| proofs, or informal proofs. |
| In items that require the student to justify, the student should not be |
| required to recall from memory the formal name of a theorem. |


| MAFS.912.G-CO.4.12 | Make formal geometric constructions with a variety of tools and <br> methods (compass and straightedge, string, reflective devices, paper <br> folding, dynamic geometric software, etc.). Copying a segment; <br> copying an angle; bisecting a segment; bisecting an angle; <br> constructing perpendicular lines, including the perpendicular bisector <br> of a line segment; and constructing a line parallel to a given line <br> through a point not on the line. |
| :--- | :--- |
| Also assesses |  |
| MAFS.912.G-CO.4.13 | Construct an equilateral triangle, a square, and a regular hexagon <br> inscribed in a circle. |
| Clarifications | Students will identify the result of a formal geometric construction. <br> Students will determine the steps of a formal geometric construction. |
| Assessment Limits | Constructions are limited to copying a segment; copying an angle; <br> bisecting a segment; bisecting an angle; constructing perpendicular <br> lines, including the perpendicular bisector of a line segment; <br> constructing a line parallel to a given line through a point not on the <br> line; constructing an equilateral triangle inscribed in a circle; <br> constructing a square inscribed in a circle; and a regular hexagon <br> inscribed in a circle. |
| Calculator | Sample Item <br> Constructions are limited to the use of a formal compass and a <br> straightedge. |
| Response Attributes | Items should not ask student to find values or use properties of the <br> geometric figure that is constructed. |
| Items may be set in a real-world or mathematical context. |  |
| group. |  |
| Items may require the student to justify why a construction results in |  |
| the geometric figure. |  |


| MAFS.912.G-GMD.1.1 | Give an informal argument for the formulas for the circumference of <br> a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use <br> dissection arguments, Cavalieri's principle, and informal limit <br> arguments. |
| :--- | :--- |
| Clarification | Students will give an informal argument for the formulas for the <br> circumference of a circle; the area of a circle; or the volume of a <br> cylinder, a pyramid, and a cone. |
| Assessment Limits | Informal arguments are limited to dissection arguments, Cavalieri's <br> principle, and informal limit arguments. |
| Items may require the student to recall the formula for the |  |
| circumference and area of a circle. |  |$|$| Items may be set in a real-world or mathematical context. |  |
| :--- | :--- |
| Items may ask the student to analyze an informal argument to |  |
| Stimulus Attributes | Items may require the student to use or choose the correct unit of <br> measure. |
| Response Attribute | Neutral |
| Calculator | See Appendix A for the Practice Test item aligned to this standard. |
| Sample Item |  |


| MAFS.912.G-GMD.1.3 | Use volume formulas for cylinders, pyramids, cones, and spheres to <br> solve problems. |
| :--- | :--- |
| Clarification | Students will use volume formulas for cylinders, pyramids, cones, and <br> spheres to solve problems. |
| Assessment Limits | Items may require the student to recall the formula for the volume of <br> a sphere. <br> Items may require the student to find a dimension. <br> Items that involve cones, cylinders, and spheres should require the <br> student to do more than just find the volume. <br> Items may include composite figures, including three-dimensional <br> figures previously learned. <br> Items may not include oblique figures. <br> Items may require the student to find the volume when one or more <br> dimensions are changed. <br> Items may require the student to find a dimension when the volume <br> is changed. |
| Stimulus Attributes | Items must be set in a real-world context. <br> Items may require the student to apply the basic modeling cycle. |
| Response Attributes | Items may require the student to use or choose the correct unit of <br> measure. <br> Items may require the student to apply the basic modeling cycle. |
| Calculator | Neutral <br> Sample Item Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-GMD.2.4 | Identify the shapes of two-dimensional cross-sections of three- <br> dimensional objects, and identify three-dimensional objects <br> generated by rotations of two-dimensional objects. |
| :--- | :--- |
| Clarifications | Students will identify the shape of a two-dimensional cross-section of <br> a three-dimensional object. <br> Students will identify a three-dimensional object generated by a <br> rotation of a two-dimensional object. |
| Assessment Limits | Items may include vertical, horizontal, or other cross-sections. <br> Items may include more than one three-dimensional shape. |
| Stimulus Attributes | Items may be set in a real-world or mathematical context. <br> A verbal description of a cross-section or a three-dimensional shape <br> may be used. |
| Response Attribute | Items may require the student to draw a line that shows the location <br> of a cross-section. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-GPE.1.1 | Derive the equation of a circle of given center and radius using the <br> Pythagorean Theorem; complete the square to find the center and <br> radius of a circle given by an equation. |
| :--- | :--- |
| Clarifications | Students will use the Pythagorean theorem, the coordinates of a <br> circle's center, and the circle's radius to derive the equation of a <br> circle. |
| Students will determine the center and radius of a circle given its |  |
| equation in general form. |  |

$\left.\begin{array}{|l|l|}\hline \text { MAFS.912.G-GPE.2.4 } & \begin{array}{l}\text { Use coordinates to prove simple geometric theorems algebraically. } \\ \text { For example, prove or disprove that a figure defined by four given } \\ \text { points in the coordinate plane is a rectangle; prove or disprove that } \\ \text { the point (1, v3) lies on the circle centered at the origin and containing } \\ \text { the point (0, 2). }\end{array} \\ \hline \text { Clarification } & \begin{array}{l}\text { Students will use coordinate geometry to prove simple geometric } \\ \text { theorems algebraically. }\end{array} \\ \hline \text { Assessment Limits } & \begin{array}{l}\text { Items may require the student to use slope or to find the distance } \\ \text { between points. }\end{array} \\ \text { Items may require the student to prove properties of triangles, } \\ \text { properties of quadrilaterals, properties of circles, and properties of } \\ \text { regular polygons. } \\ \text { Items may require the student to use coordinate geometry to provide } \\ \text { steps to a proof of a geometric theorem. }\end{array}\right\}$

| MAFS.912.G-GPE.2.5 | Prove the slope criteria for parallel and perpendicular lines and use <br> them to solve geometric problems (e.g., find the equation of a line <br> parallel or perpendicular to a given line that passes through a given <br> point). |
| :--- | :--- |
| Clarifications | Students will prove the slope criteria for parallel lines. <br> Students will prove the slope criteria for perpendicular lines. <br> Students will find equations of lines using the slope criteria for <br> parallel and perpendicular lines. |
| Assessment Limits | Lines may include horizontal and vertical lines. <br> Items may not ask the student to provide only the slope of a parallel <br> or perpendicular line. |
| Stimulus Attribute | Items may be set in a real-world or mathematical context. |
| Response Attribute | Items may require the student to be familiar with slope-intercept <br> form of a line, standard form of a line, and point-slope form of a line. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-GPE.2.6 | Find the point on a directed line segment between two given points <br> that partitions the segment in a given ratio. |
| :--- | :--- |
| Clarification | Students will find a point on a directed line segment between two <br> given points when given the partition as a ratio. |
| Assessment Limit | Items may be set in a real-world or mathematical context. |
| Stimulus Attribute | Items may require the student to find a ratio when given the <br> endpoints of a directed line segment and a point on the line segment. <br> Response Attributes <br> Items may require the student to find an endpoint when given a ratio, <br> one endpoint, and a point on the directed line segment. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-GPE.2.7 | Use coordinates to compute perimeters of polygons and areas of <br> triangles and rectangles, e.g., using the distance formula. |
| :--- | :--- |
| Clarifications | Students will use coordinate geometry to find a perimeter of a <br> polygon. <br> Students will use coordinate geometry to find the area of triangles <br> and rectangles. |
| Assessment Limits | Items may require the use of the Pythagorean theorem. <br> Items may include convex, concave, regular, and/or irregular <br> polygons. <br> In items that require the student to find the area, the polygon must <br> be able to be divided into triangles and rectangles. |
| Stimulus Attribute | Items must be set in a real-world context. |
| Response Attributes | Items may require the student to apply the basic modeling cycle. <br> Items may require the student to use or choose the correct unit of <br> measure. <br> Items may require the student to find a dimension given the <br> perimeter or area of a polygon. |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-MG.1.1 | Use geometric shapes, their measures, and their properties to <br> describe objects (e.g., modeling a tree trunk or a human torso as a <br> cylinder). |
| :--- | :--- |
| Clarifications | Students will use geometric shapes to describe objects found in the <br> real world. <br> Students will use measures of geometric shapes to find the area, <br> volume, surface area, perimeter, or circumference of a shape found <br> in the real world. |
| Students will apply properties of geometric shapes to solve real-world |  |
| problems. |  |


| MAFS.912.G-MG.1.2 | Apply concepts of density based on area and volume in modeling <br> situations (e.g., persons per square mile, BTUs per cubic foot). |
| :--- | :--- |
| Clarifications | Students will apply concepts of density based on area in modeling <br> situations. <br> Students will apply concepts of density based on volume in modeling <br> situations. |
| Assessment Limit | Items may require the student to use knowledge of other Geometry <br> standards. |
| Stimulus Attribute | Items must be set in a real-world context. |
| Response Attributes | Items may require the student to apply the basic modeling cycle. |
| Items may require the student to use or choose the correct unit of |  |
| measure. |  |


| MAFS.912.G-MG.1.3 | Apply geometric methods to solve design problems (e.g., designing an <br> object or structure to satisfy physical constraints or minimize cost; <br> working with typographic grid systems based on ratios). |
| :--- | :--- |
| Clarification | Students will apply geometric methods to solve design problems. |
| Assessment Limits | Items may require the student to use knowledge of other Geometry <br> standards. <br> Items that use volume should not also assess G-GMD.1.3 or G- <br> MG.1.1. |
| Stimulus Attribute | Items must be set in a real-world context. |
| Response Attributes | Items may require the student to interpret the results of a solution <br> within the context of the modeling situation. <br> Items may require the student to apply the basic modeling cycle. |
| Calculator | Items may require the student to use or choose the correct unit of <br> measure. |
| Sample Item | Neutral |


| MAFS.912.G-SRT.1.1 | Verify experimentally the properties of dilations given by a center and a scale factor: <br> a. A dilation takes a line not passing through the center of the dilation to a parallel line and leaves a line passing through the center unchanged. <br> b. The dilation of a line segment is longer or shorter in the ratio given by the scale factor. |
| :---: | :---: |
| Clarifications | When dilating a line that does not pass through the center of dilation, students will verify that the dilated line is parallel. <br> When dilating a line that passes through the center of dilation, students will verify that the line is unchanged. <br> When dilating a line segment, students will verify that the dilated line segment is longer or shorter with respect to the scale factor. |
| Assessment Limits | Items may use line segments of a geometric figure. <br> The center of dilation and scale factor must be given. |
| Stimulus Attributes | Items may give the student a figure or its dilation, center, and scale and ask the student to verify the properties of dilation. <br> Items may be set in a real-world or mathematical context. |
| Response Attribute |  |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test item aligned to this standard. |


| MAFS.912.G-SRT.1.2 | Given two figures, use the definition of similarity in terms of similarity <br> transformations to decide if they are similar; explain using similarity <br> transformations the meaning of similarity for triangles as the equality <br> of all corresponding pairs of angles and the proportionality of all <br> corresponding pairs of sides. |
| :--- | :--- |
| Clarifications | Students will use the definition of similarity in terms of similarity <br> transformations to decide if two figures are similar. <br> Students will explain using the definition of similarity in terms of <br> similarity transformations that corresponding angles of two figures <br> are congruent and that corresponding sides of two figures are <br> proportional. |
| Assessment Limit | Items may require the student to be familiar with using the algebraic <br> description $(x, y) \rightarrow(x+a, y+b)$ for a translation, and <br> $(x, y) \rightarrow(k x, k y)$ for a dilation when given the center of dilation. |
|  | Items may require the student to be familiar with the algebraic <br> description for a 90-degree rotation about the origin, <br> $(x, y) \rightarrow(-y, x)$, for a 180-degree rotation about the origin, |
|  | $(x, y) \rightarrow(-x,-y)$, and for a 270-degree rotation about the origin, <br> $(x, y) \rightarrow(y,-x)$ Items that use more than one transformation may <br> ask the student to write a series of algebraic descriptions. |
|  | Items may be set in a real-world or mathematical context. |
| Stimulus Attribute | Items may ask the student to determine if given information is <br> sufficient to determine similarity. |
| Response Attribute | Neutral <br> See Appendix A for the Practice Test item aligned to this standard. |
| Calculator |  |


| MAFS.912.G-SRT.1.3 <br> Also assesses MAFS.912.G-SRT.2.4 | Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar. <br> Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity. |
| :---: | :---: |
| Clarifications | Students will explain using properties of similarity transformations why the AA criterion is sufficient to show that two triangles are similar. <br> Students will use triangle similarity to prove theorems about triangles. <br> Students will prove the Pythagorean theorem using similarity. |
| Assessment Limit | Items may require the student to be familiar with using the algebraic description $(x, y) \rightarrow(x+a, y+b)$ for a translation, and $(x, y) \rightarrow(k x, k y)$ for a dilation when given the center of dilation. Items may require the student to be familiar with the algebraic description for a 90-degree rotation about the origin, $(x, y) \rightarrow(-y, x)$, for a 180-degree rotation about the origin, $(x, y) \rightarrow(-x,-y)$, and for a 270-degree rotation about the origin, $(x, y) \rightarrow(y,-x)$. Items that use more than one transformation may ask the student to write a series of algebraic descriptions. |
| Stimulus Attribute | Items may be set in a real-world or mathematical context. |
| Response Attribute |  |
| Calculator | Neutral |
| Sample Item | See Appendix A for the Practice Test items aligned to a standard in this group. |


| MAFS.912.G-SRT.2.5 | Use congruence and similarity criteria for triangles to solve problems <br> and to prove relationships in geometric figures. |
| :--- | :--- |
| Clarifications | Students will use congruence criteria for triangles to solve problems. <br> Students will use congruence criteria for triangles to prove <br> relationships in geometric figures. <br> Students will use similarity criteria for triangles to solve problems. |
| Assessment Limit | Students will use similarity criteria for triangles to prove relationships <br> in geometric figures. |
| Stimulus Attribute | Items may use geometric figures of any shape if the figure can be <br> deconstructed to form a triangle. |
| Response Attribute | Items may be set in a real-world or mathematical context. |
| Calculator | Items may require the student to use or choose the correct unit of <br> measure. |
| Sample Item | Neutral |


| MAFS.912.G-SRT.3.8 | Use trigonometric ratios and the Pythagorean Theorem to solve right <br> MAFS.912.G-SRT.3.6 <br> triangles in applied problems. |
| :--- | :--- |
| Also assesses |  |
| MAFS.912.G-SRT.3.7 | Understand that by similarity, side ratios in right triangles are <br> properties of the angles in the triangle, leading to definitions of <br> trigonometric ratios for acute angles. |
| Clarifications | Explain and use the relationship between the sine and cosine of <br> complementary angles. |
| Calculator | Students will use trigonometric ratios and the Pythagorean theorem <br> to solve right triangles in applied problems. <br> Students will use similarity to explain the definition of trigonometric <br> ratios for acute angles. |
| Sample Item | Students will explain the relationship between sine and cosine of <br> complementary angles. |
| Stimulus Attributes | Students will use the relationship between sine and cosine of <br> complementary angles. |
| Equation Editor items may require the student to use the inverse |  |
| trigonometric function to write an expression. |  |
| group. |  |
| Items will assess only sine, cosine, and tangent to determine the |  |
| length of a side or an angle measure. |  |

## Appendix A

The chart below contains information about the standard alignment for the items in the Geometry Computer-Based Practice Test at http://fsassessments.org/students-and-families/practice-tests/ .

| Content Standard | Item Type | Computer-Based Practice Test Item Number |
| :---: | :---: | :---: |
| MAFS.912.G-C.1.1 | Equation Editor | 14 |
| MAFS.912.G-C.1.2 | Equation Editor | 3 |
| MAFS.912.G-C.1.3 | GRID | 12 |
| MAFS.912.G-C.2.5 | Equation Editor | 23 |
| MAFS.912.G-C.2.5 | Multiple Choice, Equation Editor, and Equation Editor | 33 |
| MAFS.912.G-CO.1.1 | Open Response | 7 |
| MAFS.912.G-CO.1.2 | Table Item | 18 |
| MAFS.912.G-CO.1.4 | Editing Task Choice | 4 |
| MAFS.912.G-CO.1.3 | Multiselect | 8 |
| MAFS.912.G-CO.2.6 | Multiple Choice | 10 |
| MAFS.912.G-CO.2.8 | Multiple Choice, GRID, and Editing Task Choice | 32 |
| MAFS.912.G-CO.3.9 | Equation Editor | 1 |
| MAFS.912.G-CO.3.9 | Drag and Drop Hot Text | 11 |
| MAFS.912.G-CO.3.10 | Drag and Drop Hot Text | 21 |
| MAFS.912.G-CO.3.11 | Drag and Drop Hot Text | 5 |
| MAFS.912.G-CO.4.12 | Multiple Choice | 27 |
| MAFS.912.G-GMD.1.1 | Multiselect | 9 |
| MAFS.912.G-GMD.1.3 | Equation Editor | 28 |
| MAFS.912.G-GMD.2.4 | Multiple Choice | 16 |
| MAFS.912.G-GPE.1.1 | Editing Task Choice | 6 |
| MAFS.912.G-GPE.2.4 | Editing Task Choice | 25 |
| MAFS.912.G-GPE.2.5 | Equation Editor | 15 |
| MAFS.912.G-GPE.2.6 | Equation Editor | 20 |
| MAFS.912.G-GPE.2.7 | Equation Editor | 26 |
| MAFS.912.G-MG.1.1 | Matching Item | 2 |
| MAFS.912.G-MG.1.2 | Equation Editor | 30 |
| MAFS.912.G-MG.1.3 | Equation Editor | 24 |
| MAFS.912.G-SRT.1.1a | Multiselect | 22 |
| MAFS.912.G-SRT.1.2 | Multiselect | 17 |
| MAFS.912.G-SRT.2.4 | Multiple Choice | 13 |

Geometry EOC Item Specifications
Florida Standards Assessments

| Content Standard | Item Type | Computer-Based Practice Test <br> Item Number |
| :---: | :---: | :---: |
| MAFS.912.G-SRT.2.4 | Drag and Drop Hot Text | 19 |
| MAFS.912.G-SRT.2.5 | Editing Task Choice | 29 |
| MAFS.912.G-SRT.3.8 | Equation Editor | 31 |

## Appendix B: Revisions

| Page(s) | Revision | Date |
| :---: | :---: | :---: |
| $42-43$ | Appendix A updated to show Fall 2018 Practice Test information | September 2018 |

## Geometry EOC FSA Mathematics Reference Sheet

## Customary Conversions

1 foot $=12$ inches
1 yard = 3 feet
1 mile $=5,280$ feet
1 mile $=1,760$ yards
1 cup $=8$ fluid ounces
1 pint $=2$ cups
1 quart $=2$ pints
1 gallon $=4$ quarts

1 pound $=16$ ounces
1 ton = 2,000 pounds

## Metric Conversions

1 meter = 100 centimeters
1 meter $=1000$ millimeters
1 kilometer $=1000$ meters

1 liter = 1000 milliliters

1 gram = 1000 milligrams
1 kilogram = 1000 grams

## Time Conversions

1 minute $=60$ seconds
1 hour $=60$ minutes
1 day $=24$ hours
1 year $=365$ days
1 year = 52 weeks

## Geometry EOC FSA Mathematics Reference Sheet

## Formulas

$\sin A^{\circ}=\frac{\text { opposite }}{\text { hypotenuse }}$
$\cos A^{\circ}=\frac{\text { adjacent }}{\text { hypotenuse }}$
$\tan A^{\circ}=\frac{\text { opposite }}{\text { adjacent }}$
$V=B h$
$V=\frac{1}{3} B h$
$V=\frac{4}{3} \pi r^{3}$
$y=m x+b$, where $m=$ slope and $b=y$-intercept
$y-y_{1}=m\left(x-x_{1}\right)$, where $m=$ slope and $\left(x_{1}, y_{1}\right)$ is a point on the line

